#### **§2.7 Inverse Functions**

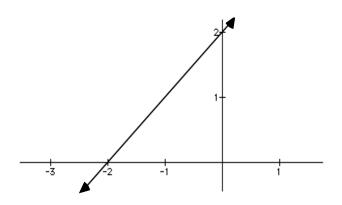
Example: Let f(x) = 8x and  $g(x) = \frac{1}{8}x$ 

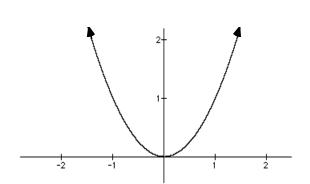
Find f(12) and g(96)? What do you notice about these results?

#### **Horizontal Line Test:**

A function f has a inverse function if and only if no horizontal line intersects the graph of f at more than one point.

Example: Do the following graphs of functions have inverses?





### **Inverse Function**

Let f and g be two functions such that:

 $(f \circ g)(x) = x$  for every x in the domain of g,

and  $(g \circ f)(x) = x$  for every x in the domain of f.

The function g is the **inverse** of the function f and is denoted by  $f^{-1}(x)$  where

 $f(f^{-1}(x)) = x$  and  $f^{-1}(f(x)) = x$ .

Example: Let  $f(x) = x^3 - 1$ , and let  $g(x) = \sqrt[3]{x+1}$ . Is g the inverse of f?

## Finding the Inverse of a function:

Note: the notation used is:  $f^{-1}(x)$ 

- Verify that f has an inverse by the horizontal line test.
- Replace f(x) with y.
- •Interchange the variables x and y.
- Solve for y and let this "new"  $y = f^{-1}(x)$
- Verify that  $f(f^{-1}(x)) = x$  and  $f^{-1}(f(x)) = x$ .

Example Find the inverse of the following functions.

a.) 
$$f(x) = 2x-1$$
 b.)  $f(x) = \frac{4x+6}{5}$ 

# **Graphs of Inverses:**

(A graph and it's inverse are symmetric with respect to the line y = x.)

