Guidelines for Graphing Rational Functions

a.) $f(x) = \frac{2(x^2 - 9)}{x^2 - 4}$ example Find and plot the x-intercepts. (Set numerator = 0 and solve for x). $2(x^2 - 9) = 0$ $x^2 - 9 = 0$ $x^2 = 9$ $x = \pm 3$

2. Find and plot the v-intercepts. (Let x = 0 and solve for y)

$$f(0) = \frac{2(0^2 - 9)}{0^2 - 4} = \frac{9}{2}$$

3. Find and plot the Vertical Asymptotes. (Set denominator = 0 and solve for x)

$$x^2 - 4$$

1.

$$X = 4$$

$$x = \pm 2$$

Find and plot the Horizontal Asymptotes. (Top heavy, Bottom heavy or Same) 4.

 $f(x) = \frac{2(x^2 - 9)}{x^2 - 4}$ Rule 2 Numerator and denominator have the same degree. y = 2 H.A.

Find and plot the Slant Asymptotes. (Divide numerator by denominator.) 5.

None ! Only have these if Numerator is exactly 1 degree higher than denominator!

Find where the graph will intersect its nonvertical asymptote by solving f(x) = k, where k is the y-6. value of the horizontal asymptote, or f(x) = mx + b, where y = mx + b is the equation of the oblique asymptote.

Solve $2 = \frac{2(x^2 - 9)}{x^2 - 4}$ (No solution!) No oblique asymptotes.

7 Plot at least one point between and beyond each x-intercept and vertical asymptotes.

Remember Test Points ?

Choose test points carefully!

x = -4	x = -2.5	$\mathbf{x} = 0$	x = 2.5	x = 4		x = -1	x = 1	
y = 1.16	y = -2.4	y = 4.5	y = -2.4	y = 1.16		y = 5.3	y = 5.3	

Note: YOU STILL MAY HAVE TO PLOT ADDITIONAL POINTS !

Use smooth curves to complete the graph between and beyond the vertical asymptotes.



Example Sketch the graph and provide information about intercepts and asymptotes.

$$f(x) = \frac{x}{x^2 - x - 2}$$

1. Find and plot the x-intercepts. (Set numerator = 0 and solve for x)

$$\mathbf{x} = \mathbf{0}$$

2. Find and plot the y-intercepts. (Let x = 0 and solve for y)

 $f(0) = \frac{0}{0^2 - 0 - 2} = 0$

3. Find and plot the Vertical Asymptotes. (Set denominator = 0 and solve for x)

 $x^{2} - x - 2 = 0$ (x + 1)(x - 2) = 0 x = -1 and x = 2

4. Find and plot the Horizontal Asymptotes. (Top heavy, Bottom heavy or Same)

(Rule 1) y = 0

5. Find and plot the Slant Asymptotes. (Divide numerator by denominator.) None

6. Plot at least one point between and beyond each x-intercept and vertical asymptotes.

choose:

 $\begin{array}{c|cccc} x = -2 & x = -.5 & x = 1 \\ y = -.5 & y = .4 & y = -.5 & y = .75 \end{array}$

Note: YOU MAY WANT TO PICK MORE POINTS TO GET A BETTER GRAPH !



ANSWER: