

Directions: To receive partial credit you must show your work on a problem.

Circle final answers. All problems are 5 points each.

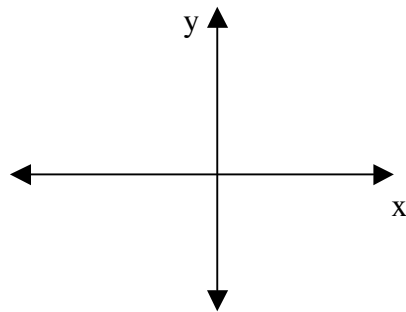
For the quadratic function $y = -2x^2 - 12x - 16$ find the following.

1. Vertex = _____

2. x and y intercepts
x-int = _____ y-int = _____

For the quadratic function $y = -2x^2 - 12x - 16$ find the following.

3. Graph



4. Domain and Range

D = _____ R = _____

Divide the following polynomials.

5. $(2x^2 + 10x + 12) \div (x + 3)$

Divide the following polynomials.

6. $(4x^3 - 7x^2 - 11x + 5) \div (4x + 5)$

Divide the following polynomials.

7. $(5x^3 - 6x^2 + 8) \div (x - 4)$

Divide the following polynomials.

8. $(7x + 3) \div (x + 2)$

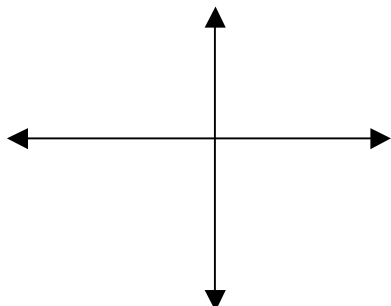
Use synthetic division and the factor theorem to determine whether the second polynomial is a factor of the first. State **YES** or **NO**

9. $f(x) = x^4 - 25x^2 + 144; \quad x + 3$

Describe the transformation that occurs in the function. Remember to find the basic function first. Also sketch the graph.

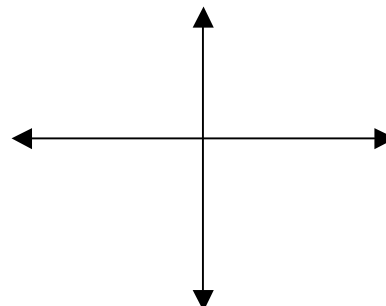
10. $f(x) = -x^4 + 4$

Description: _____



11. $f(x) = (x - 2)^3 - 2$

Description: _____

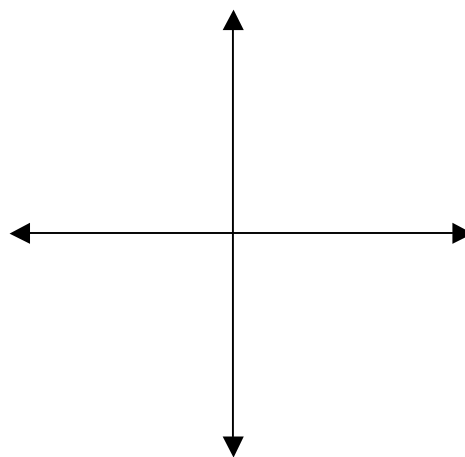


Graph the polynomial function. **SHOW ALL** the steps we discussed in class.

$$y = (x + 2)(x - 1)(x - 2)(x + 2)$$

12. Find the x and y intercepts.
13. Find the test point information for the x-intercepts.

14. Use the previous work(#12 and #13) to graph the polynomial.



Find the zeros of the polynomial and state the multiplicity of each.

15. $P(x) = x^2(x^2 - 4)(x + 3)^2$

Use the Rational Zero Theorem to list possible rational zeros for the polynomial.

16. $P(x) = 2x^3 + x^2 - 25x + 12$

Use the Rational Zero Theorem to list possible rational zeros for the polynomial.

17. $P(x) = x^5 - 32$

Factor each polynomial into linear factors and/or quadratic factors that are irreducible over the reals.

18. $P(x) = x^3 - x^2 - 2x$

Find the zeros of the polynomial.

19. $P(x) = 2x^4 - 17x^3 + 4x^2 + 35x - 24$

Find the zeros of the polynomial.

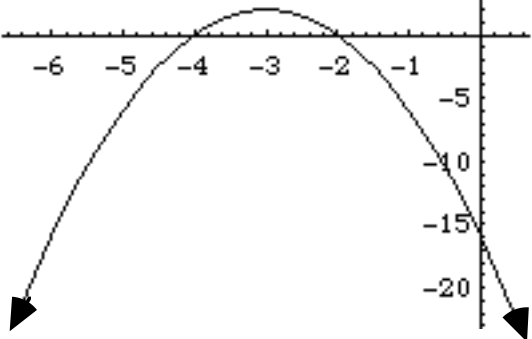
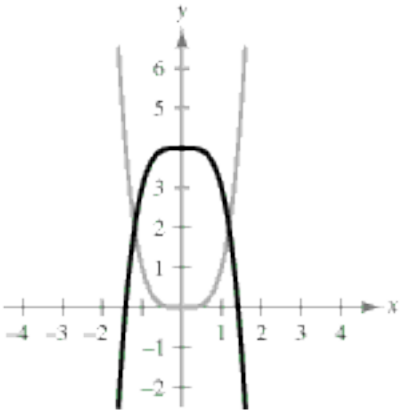
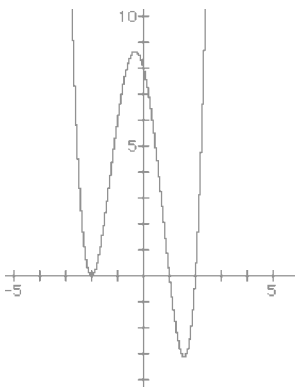
Hint: Find the rational zeros first.

20. $P(x) = x^4 + x^3 - 2x^2 + 4x - 24$

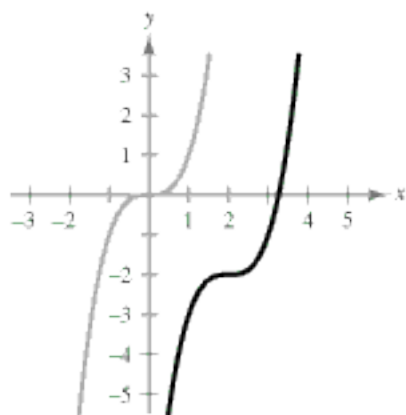
Find the zeros of the polynomial.

21. $P(x) = 6x^4 + 23x^3 + 19x^2 - 8x - 4$

Answers Sample Test 3

1. vertex: $(-3, 2)$	2. x - int.: $(-4, 0), (-2, 0)$ y - int.: $(0, -16)$
3. 	4. Domain = $(-\infty, \infty)$ Range = $(-\infty, 2]$
5) $2x + 4$ 6) $x^2 - 3x + 1$ 7) $5x^2 + 14x + 56 + \frac{232}{x - 4}$ 8) $7 - \frac{11}{x + 2}$ 9) Yes! Remainder is zero!	12) x-int: $x = -2, x = 1, x = 2, x = -2$ y-int: $y = 8$ 13) Answers may vary. $x = -3, y = 20$ <u>above x-axis</u> $x = 0, y = 8$ <u>above x-axis</u> $x = 1.5, y = -3.06$ <u>below x-axis</u> $x = 3, y = 50$ <u>above x-axis</u>
10.  Reflection in the x-axis and then a vertical shift four units upward.	14)  15) 0 is a zero of multiplicity two 2 is a zero of multiplicity one -2 is a zero of multiplicity one -3 is a zero of multiplicity two

11.



Horizontal shift two units to the right and a vertical shift two units downward.

$$16) \quad \frac{p}{q} = \pm 1, \pm 2, \pm 3, \pm 4, \pm 6, \pm 12, \pm \frac{1}{2}, \pm \frac{3}{2}$$

$$17) \quad \frac{p}{q} = \pm 1, \pm 2, \pm 4, \pm 8, \pm 16, \pm 32$$

$$18) \quad \text{factors are: } x(x-2)(x+1)$$

$$19) \quad \text{zeros are: } x = 8, x = 1, x = 1, x = -\frac{3}{2}$$

$$20) \quad \text{zeros are: } x = -3, x = 2, x = +2i, x = -2i$$

$$21) \quad \text{zeros are: } x = \frac{1}{2}, x = -2, x = -2, x = -\frac{1}{3}$$