

§5.1 Exponential Functions and Their Graphs

Exponential Function:

If $a > 0$, $a \neq 1$, and x is any real number, then

$f(x) = a^x$ defines the **exponential function** with base a .

Example 1 : Evaluate the following exponential expressions with your calculator.

a) $2^{-3.1}$

b) 2^π

Graphing Exponential Functions

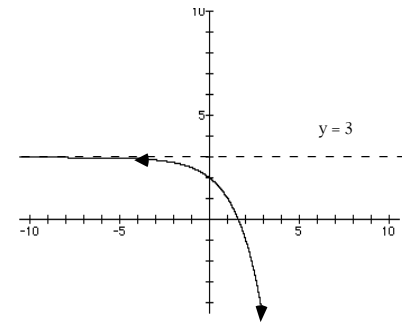
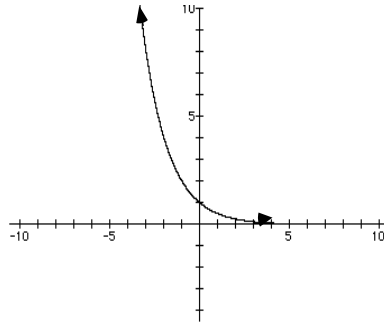
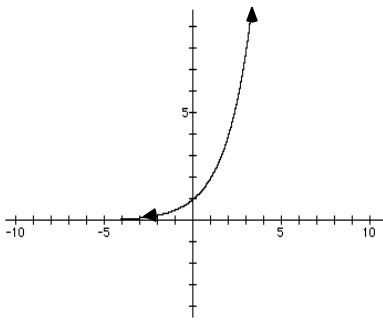
Graphs of the Form: $f(x) = a^x$

- 1) The point $(0, 1)$ is on the graph.
- 2) If $a > 1$, f is an increasing function; If $0 < a < 1$, f is a decreasing function.
- 3) The x -axis is a horizontal asymptote.
- 4) The domain is $(-\infty, \infty)$ and the range is $(0, \infty)$.

Graph $f(x) = 2^x$

Graph $g(x) = 2^{-x}$

Graph $h(x) = -2^x + 3$



Horizontal Asymptote: The line in which a graph approaches (gets closer and closer to)

Increasing Function: A function where as x-values increase so do the y-values.

Decreasing Function: A function where as x-values increase y-values decrease.

Exponential Equations (TYPE 1)

Example 2: Solve

$$\text{a) } \left(\frac{1}{3}\right)^x = 81$$

$$\text{b) } 1.5^{x+1} = \left(\frac{27}{8}\right)^x$$

The Natural Base e

$$e \approx 2.71828\dots$$

Example 3: Use a calculator to evaluate each expression.

$$\text{a) } e^{-2}$$

$$\text{b) } e^{-1}$$

$$\text{c) } e^1$$

$$\text{d) } e^2$$

Formulas for Compound Interest:

After t years, the balance A in an account with principal P and annual interest rate r (in decimal form) is given by the following formulas:

1. For n compoundings per year:

$$A = P \left(1 + \frac{r}{n} \right)^{n \cdot t}$$

2. For continuous compounding:

$$A = Pe^{r \cdot t}$$

Example 4: A total of \$12,000 is invested at an annual interest rate of 9%. Find the balance after 5 years if it is compounded:

a) quarterly.

b) continuously.