

## §5.5 Applications and Modeling with Exponential and Logarithmic Functions

### Exponential Growth or Decay Function :

Let  $a$  be the amount or number present at time  $t = 0$ . Then, under certain conditions, the amount present at any time  $t$  is given by  $y = ae^{bt}$  where  $b$  is a constant.

-the number  $b$  is the rate of growth or decay.

-if  $b > 0$ , the function describes growth; if  $b < 0$ , the function describes decay.

- the **doubling time** of a quantity that grows exponentially is the amount of time that it takes for any initial amount to grow to twice that amount  $y = 2a$

- the **half-life** of a quantity that decays exponentially is the amount of time that it takes for any initial amount to decay to half that amount  $y = (1/2)a$

Example 1: A sample of 300 grams of radioactive plutonium 241 decays according to the function  $A(t) = 300 e^{-.053t}$ , where  $t$  is time in years.

a.) Find the amount of the sample remaining after 5 years.

b.) Find the half-life of plutonium 241.

Example 2: A model of the world population (in millions) is given by  $P(t) = 4451e^{0.017303t}$  where  $t = 0$  represents 1980. According to this model, when will the world population reach 6 billion?

### **Continuous Compounding:**

If  $P$  dollars is deposited at a rate of interest  $r$  compounded continuously for  $t$  years, the final amount on deposit is  $A = Pe^{rt}$  dollars.

Example 3: Suppose \$5000 is deposited in an account paying 3% interest compounded continuously for 5 years. Find the total amount on deposit at the end of five years.

Example 4: How long will it take for the money in an account that is compounded continuously at 3% to double ?