§ 1.6 Shifting, Reflecting, and Stretching Graphs

Shifting Graphs (Rigid Translations) - given a function y = f(x) and c > 0

(1) the graph of y = f(x) + c is the graph of y = f(x) shifted up c units.

(2) the graph of y = f(x) - c is the graph of y = f(x) shifted down c units.

(3) the graph of y = f(x + c) is the graph of y = f(x) shifted left c units.

(4) the graph of y = f(x - c) is the graph of y = f(x) shifted right c units.

Example 1: Graph.

a.)
$$y = |x| + 2$$

b.)
$$y = |x| - 2$$

c.)
$$y = |x + 2|$$

d.)
$$y = |x - 2|$$

Reflecting Graphs - given a function y = f(x)

- the graph of y = -f(x) is the graph of y = f(x) reflected over the x-axis. (1)
- (2) the graph of y = f(-x) is the graph of y = f(x) reflected over the y-axis.

Example 2: Graph. a.) $y = -\sqrt{x}$

a.)
$$y = -\sqrt{x}$$

b.)
$$y = \sqrt{-x}$$

Narrowing and Broading (Non-Rigid Translations):

The graph of g(x) = c * f(x) has the same general shape as the graph of f(x).

- 1) It is narrowed vertically compared to the graph of f(x) if c > 1.
- 2) It is broadened vertically compared to the graph of f(x) if 0 < c < 1.

Example 3: Graph. a.) y = 5 |x|

a.)
$$y = 5 |x|$$

b.)
$$y = \frac{1}{2} |x|$$

(Note: when an equation contains more than one shifting or reflecting rule, use steps (one rule at a time) and work from the inside of the function to the outside.)