

## §5.4 Sum and Difference Formulas

**REMEMBER YOU KNOW ALGEBRA !**

### Sum or Difference of Two Angles Identities

$$\cos(\alpha - \beta) = \cos \alpha \cos \beta + \sin \alpha \sin \beta$$

$$\cos(\alpha + \beta) = \cos \alpha \cos \beta - \sin \alpha \sin \beta$$

$$\sin(\alpha - \beta) = \sin \alpha \cos \beta - \cos \alpha \sin \beta$$

$$\sin(\alpha + \beta) = \sin \alpha \cos \beta + \cos \alpha \sin \beta$$

$$\tan(\alpha + \beta) = \frac{\tan \alpha + \tan \beta}{1 - \tan \alpha \tan \beta}$$

$$\tan(\alpha - \beta) = \frac{\tan \alpha - \tan \beta}{1 + \tan \alpha \tan \beta}$$

### Cofunction Identities

$$\sin(90^\circ - \theta) = \cos \theta$$

$$\cos(90^\circ - \theta) = \sin \theta$$

$$\csc(90^\circ - \theta) = \sec \theta$$

$$\sec(90^\circ - \theta) = \csc \theta$$

$$\tan(90^\circ - \theta) = \cot \theta$$

$$\cot(90^\circ - \theta) = \tan \theta$$

Example 1 Find the exact value.

$$\cos 75^\circ$$

Example 2 Find the exact value.

$$\sin \frac{\pi}{12}$$

Example 3 Find the exact value.

$$\sin 42^\circ \cos 12^\circ - \cos 42^\circ \sin 12^\circ$$

Example 4 Prove a Cofunction

$$\cos \frac{\pi}{2} - x$$

Example 5 Simplify.

$$\tan(\theta + 3)$$

Example 6 Given  $\cos \alpha = \frac{8}{17}$ ,  $\alpha$  in quadrant IV, and  $\sin \beta = -\frac{24}{25}$ , in quadrant III, find

$$\cos(\alpha + \beta)$$